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XXXVI. A View of the Relation between the celebrated Dr. Halley's Tables, and the Notions of Mr. De Buffon, for establishing a Rule for the probable Duration of the Life of Man; by Mr. William Kersseboom, of the Hague. Translated from the French, by James Parsons, M. D. and F. R.S.

eo disconvenit inter

Meque et te -

Read May 31, § 1. Y fituation in life not permitting me to look over the works of the learned, was the reason, why I was not one of the first, who perused the General and particular Natural History, &c. of Mr. de Busson. However a little interval of leisure allowing me to look into it, I am at a stand to find myself mention'd, in the same breath with the celebrated Dr. Halley and others, to receive our condemnation on account of the tables for determining the degrees of probability of the duration of human life: and as this passage is the occasion of my remarks, I will begin by citing it intirely here:

"Man (says M. de Buffon, at the end of the fecond tome) as is well known, dies at all ages; and altho' it may be said in general, that his life is longer than that of almost any other animal, it cannot be denied, that it is at the same time more variable and uncertain. Attempts have been of late years made to know the degrees of these variations,

" and to establish, by observations, some certainty " concerning the mortality of mankind of different " ages. If these observations were sufficiently exact, " and a fufficient number of them made, they would " be of very great use towards knowing the number " of the people, of their increase, of the consumption " of provisions, of the division of taxes, &c. Many " ingenious men have studied this subject; and lately " Mr. Deparcieux, of the Academy of Sciences, has " given us an excellent work, which ferves as a rule " for the future, with respect to annuities for life: " but, as his principal view was to calculate the mor-"tality of annuitants, and that, in general, annuitants " for life are men in one state, no conclusion can be " drawn from it for the mortality of mankind at "large. The tables, which he has given in the " same work upon the mortality of the different re-" ligious orders, are also very curious; but, being con-" fined to a certain number of men, who live in a " different manner from others, they are not yet suf-" ficient to found exact probabilities with relation " to the general duration of life.

"Dr. Halley, Messieurs Graunt, Kersseboom, Sympson, &c. have also published tables of the mortality of mankind; and they have sounded them upon extracts from the bills of mortality of some parishes of London, Breslaw, &c. But it appears to me, that their researches, however ample, and the result of long study, can afford only very distant approaches to the knowlege of the mortality of mankind in general. In order to make a good table of this kind, not only the registers of the parishes of such a city as London, Paris, &c.

"fhould be made use of, where foreigners are daily coming in, and natives going out, but also those of the country; that, by adding together the refults of each, the one may compensate the other. M. Dupré, de St. Maur, of the French Academy, has begun this upon twelve country parishes, and three of those of Paris: he was willing to communicate these tables to me to publish them; and I the more readily do it, because they are the only tables, upon which the probabilities of the life of mankind in general can be establish'd with any certainty.".

As for the tables, I refer for them to the work.

§ 2. I am not at all concern'd for a defence of my table, which is sufficient to support itself; but I am greatly furprifed, that a philosopher should condemn works, which he never either faw or read: for it is evident, M. de Buffon never saw my Essays on political Arithmetic; and that all, which he appears to know of it, is indeed very flightly drawn from M. Deparcieux's work, who nevertheless knew no more of it, as he himself makes it appear, than what he found in the Bibliotheque raisonnée for the first three months of the year 1743, Tom. 30. This extract happens unluckily not to be made by an able hand; but, on the contrary, very fit, by its confusion, and the irregularities, which run thro' it, to lead into errors. The corrections, that were made in the fecond part of the same 30th Tome, are not even sufficient to secure the reader from mistakes.

Nevertheless M. de Buffon, without even reading the work, might have known more of it, though H h written

written in a language, which he is very likely a stranger to; since Mr. Eames has given an excellent extract of the first essay in English, printed in No 450 of the Transactions of the Royal Society of London, of which this philosopher is a member; and also because Mr. Van Rixtel has inserted an extract of the two fucceeding ones in No 468. of the faid Transactions. Besides which, M. de la Chapelle has given, in his 13th Tome of the Nouvelle Bibliotheque for the month of December in the year 1742, a very ample and judicious extract of the three essays together. I have also confirm'd my observations by a very interesting and sensible proof, upon that part of London called the city, which is printed in the first three months of the year 1743, Tom. 14. of the Nouvelle Bibliotheque; and likewise in the second three months of the year 1745 of the Bibliotheque raisonnée, is inserted a small piece relative to my observations and proofs. I take the liberty of referring every reader, who may not understand the Low-Dutch language, to those several pieces cited; and my table of the degrees of the probability of the duration of the life of man will fupport itself very well against the hasty judgment of M. de Buffon, who certainly has too much candour not to acknowlege, after a mature deliberation of those pieces mention d, that they contain fomething more than " very distant approaches to the knowlege of the " mortality of mankind in general."

§ 3. I would say much the same of that excellent piece of the learned Dr. Halley, if my surprize did not increase, the more I reslect, that this work ought to be thoroughly known to a member of the Royal Society of London; and that this very member nevertheless makes so careless a judgment upon

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it. This reflection leads me to another kind of defence of that famous deceased author; which is to make M. de Buffon sensible, that "nearly the same degrees of probability of the duration of the life of man in general" are in the table of Dr. Halley, which he would have us think are in the extracts of M. Dupré's observations or tables, which he has published. For this purpose I constructed a table parallel to that of Dr. Halley, which begins with 1000 lives of one year old, and which I found, in the reduction of the great general numbers of Dupré's tables, to have also the smaller numbers analogous; that is, by beginning also with 1000 lives of a year old. Both tables are laid down as follows:

_Ha	dley's	Table.		Dupr	é's, rec	luced.
Years	Num-	Number of	1	Years	Num-	Number of
of	ber of	Deaths fr.		of	ber of	Deaths fr.
Age	Lives	Year to Yr.		Age	Lives	Year to Yr.
I	1000			I	1000	
e.	855	145		2	864	136
3	798	57 38 28		-	808	56
3 4 5 6	760	38			768	40
4	-	28		4		29
5	732	22	·	5	739	
6	710	18		3 4 5 6	716	23
7	692	1			699	17
7 8	680	12		7 8	685	14
9	670	10			676	9 6
	199	9		9		6
10		9 8		10	670	
11	653			11	665	5
I 2	646	/	-	12	659	1
13	640	7 6 6 6 6		13	655	4
14	634	0		14	651	4
15	628	0		15	64.6	4 5 6
16	622	0		16	640	
1	1	6	•	10	040	6
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Dupre's, reduc'd.

Years	Num-	Number of		Years	Num-	Number of
of	ber of	Deaths fr		of	ber of	Deaths fr.
Age	Lives	Year to Yr		Age	Lives	Year to Yr.
-			,		-	
17	616	6		17	634	6
18	610			18	628	1
19	604	. 6		19	622	6 8
20	598	6		20	614	
21	592	6 6 6		2 I	609	5 10
22	586	1		22	599	
23	579	6		23	592	/
24	573 567 560	6 6	İ	24 25 26	592 585	IF
25 26	507		1	25	574	Q
26	560	7		26	566	Q
27 28	553	7 7 7 8 8 8 8		27	558	7 7 1 r 8 8 8
28	546	7		28	550	6
29	1 539	8		29	544	l _
30 31 32 33 34 35 36 37 38 39 40	531 523	8		30	531 526 516 508	13
31	523	l g		30 31 32 33 34 35 36 37 38 39 40	526	5 10 8 7 16
32	515	8		32	516	2
33	507	8		33	508	7
34	499			34	501	76
35	490	9		35	485	10
36	481	9		36	475	1
37	472	9		37	475 466	9
38	463	9		38	457	9 5 23
39	454	9		39	452	5
40	445	9		40	429	23
41	445 436	9 9 9 9 9 9 9 9		41	424	5 J1
4.2	427	9		42	413	
43	417	9		43	406	7 6
44	497	10		44	400	0
77	1 77	10	F 1	1 17	1	8 r

Halley's

Halley's Table.	Hall	ey's	Ta	ble.
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Halle	y's Table.		Dupr	é's, re	duced.
of ber	Number of Deaths fr. Year to Yr.		Years of Age	Num- ber of Lives	Number of Deaths fr. Year to Yr.
45 35 46 38 47 37 48 36 50 34 51 33 52 32 53 31 54 36 55 28 57 29 56 28 57 29 60 22 61 22 63 2 64 65 1	77 10 77 10 77 10 77 10 77 10 77 11 11 11 11 12 11 10 10 10 10 10 10 10 10 10 10 10 10		Age 45 46 47 48 49 50 51 52 53 54 55 57 58 59 60 61 62 63 64 65 66 67	382 374 368 359 353 327 318 306 322 283 276 265 225 215 206 197 184 171 164	8 6 9 6 21 5 9 5 7 4 19 7 11 5 30 5 10 9 13 13 13
68 1	62 10		68	151	6
70 1	42 10		70	123	6
	31 11		71 72	117	15
1	1 11	1	1	5	7

Halley's

Halley's Table	٥.	
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Dupre's, reduc'd.

		Number of Deaths fr. Year to Yr	Years of Age	Num- ber of Lives	Number of Deaths fr. Year to Yr.
73 74 75 76 77 78 79 80 81 82 83 84	109 98 88 78 68 58 49 41 34 28 23	11 10 10 10 10 9 8 7 6 5	73 74 75 76 77 78 79 81 82 83 84	95 86 71 65 58 49 46 32 29 24 20	9 15 6 7 9 3 14 3 5 4 3

Sum total of Dr. Halley's table . . . 34000 Sum total of M. Dupré's table reduced . 33911

In the whole matter, all the difference between these two tables consists in this, that Dr. Halley's is more perfect, more compact, and more conformable to those observations, which conduct us all to the idea of a progression nearly arithmetical, which the great number of researches enables us to unfold by little and little, in the representation of the strength of human life, when that strength is become more uniform.

§ 4. If M. de Buston will compare the table given by himself of the probability of the duration of life, which is founded upon that of M. Dupré de St. Maur, with

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with that given by M. Deparcieux, in his ingenious work constructed upon that of Dr. Halley, he will find a like conformity between them. It is M. Deparcieux's thirteenth table, which I have before me. What follows, in Halley's column, I set down, in order to compare it with M. de Buffon's table.

Deparcieux upon Halley.				De Buffon upon Dupré of St. Maur.				
Years of Age		at a Me- um. Mºs.				Years of Age	1	ation of life. Months
1 2 3 4 5	33 38 39 40 41	60993				1 2 3 4 5	33 38 40 41 41	6
6 7 8 9						6 7 8 9	42 42 41 40	3 6 10
10 11 12 13 14 15	37	5				10 11 12 13 14 15	39 38 38 37 36	6 9 1 5
•		•	•			•		rcieux

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Deparcieux upon Halley.

De Buffon upon Dupré of St. Maur.

Years	Lives at a	Medium.		Years	Duratio	n of Life.
of Age	Years	Months		of Age	Years	Months
16				16	36	0
17			•	17	35	4
17	•		1	18	34	4 8
19				19	34	o
20	34	2		20	33	5
2 I				21	32	11
22			ľ	22	32	4
23				23	31	10
24	. .	1		24	31	
25	30	II		25	30	3 9
26				26	30	$oldsymbol{z}$
]		27	29	
27 28		1		28	29	7 0 6
29				29	28	6
30	27	11		30	28	O
31				31	27	6
32		1		32	26	11
33				33	26	
34		1	1	34	25	3 7 0
35	25	0		35	25	0
26			·	36	24	5
27				37	23	10
36 37 3 8	:			37 38	23	3
9		•				parcieux

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Deparcieux upon Halley.

De Buffon upon Dupré of St. Maur.

Years of	Duration	of Life.		Years	Duratio	n of Life.
Age.	Years.	Months.		of Age.	Years.	Months.
39				39	22	8
40	22	4		40	22	1
41				41	21	6
42				42	20	11
43			ľ	43	20	4
44				44	19	9
45	19	8	d.	45	19	3
46				46	18	9
47			}	47	18	2
48				48	17	8
49				49	17	2
50	17	3		50	16	7
51				51	16	0
52	J			52	15	6
53				53	15	0
54			.	54	14	6
<i>55</i>	14	10		55	14	0
56				56	13	5
57				57	12	IÓ
58				58	12	1
59				59	11	8
60	12	5		60	11	r
	j	•	¹ I i	1 .	D	। eparcieux

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Deparcieux upon Halley.

De Buffon upon Dupre of St. Maur.

Years of	Duration	of Life.	Years of	Duration	of Life.
Age.	Years.	Months.	Age.	Years.	Months.
бı			61	10	6
62			62	10	6
63 64	·		63 64	9	6
64		-	64	9 9 8	6
65	9	71	65	8	6
66		·	66	8	0
67			67		6
67			67 68	7 6 6	0
69			69	6	
70	7	7	70	6	7 2
71			71	· g .	8
72			72	5 5 4 4	
73			72 73	5	4 0
74	1	•	74	4	9
75	5	7	75	4	6
76	l		76	4	3
76 77 78			77	4	I
78			77 78	3	11
79	İ		79	ž	9
79	4	6	79 80	4 3 3 3	9
81]	I	81	2	*
82	I	i	82	3 3 3	5 3 2 1
83			82	3	2
84 l	3	6	84	ž	1

§ 5. It is therefore sufficiently demonstrated, that Dr. Halley's table ought not, in M. de Buffon's opinion, to be excluded from the class of those, which are the only tables, upon which the probabilities of the life of mankind in general can be established with any certainty; far from being comprised, in his severe judgment, among those of authors, whose researches, however ample, and the result of long study, can afford only distant approaches to the knowlege of the mortality of mankind in general.

§ 6. M. de Buffon begins his table of the probabilities of life with a term, which precedes that of a year old, called zero d'age; and from M. Dupré's observations, affigns to it a duration of 8 years. thought it an error of the press; but there is no room for this doubt, after what M. de Buffon fays, "We " fee by this table (fays he) that one may reason-" ably hope, that is, lay an even wager, that an in-"fant just born, or who has no age, will live eight " years: that an infant, who is a year old, will live " thirty-three years," &c. This little space of eight vears struck me; because all the observations, which I know, are very far from it. I had therefore recourse to the source, to the observations of Mr. Duprê himself, and I found it was a mistake of M. de Buffon: the mean life of infants of no age being, according to M. Dupré's tables, twenty-and-five years and up-ward; and, from the observations of Justel, which Dr. Halley made use of, the mean life of a child of no age is above twenty-and-seven years.

§ 7. I might make an end here, if the subject did not absolutely require my offering a word concerning the nature of both Justel's and M. Dupré's observations.

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The remark has not escaped the sagacity of Dr. Halley himself: it is, "that they want the essential; "which is, the number of living persons, among "whom the observations upon the dead are made." If M. de Busson had made the same reslections upon M. Dupré's tables, he would have found the irreparable desect of them, as well as Dr. Halley did in Justel's observations; and he would have attended more, without doubt, to the method proposed by Mons.

Deparcieux.

§ 8. I shall put an end to this treatise by a word or two, which relates to Dr. Short's displeasure against me. This may perhaps be unnecessary, after the laborious and judicious extract of his book in the Journal Britannique, of the month of July 1750. However since Dr. Short joins with those, who inconsiderately have accused me of partiality to such or such a city, he will have with them my defence (to say no more) in my letter to Mr. Eames, and in the piece already quoted in the Nouvelle Bibliotheque, Tom. XIV. Artic. 8. Let him read, and he will return from his prejudice: if not,

Curentur dubii medicis majoribus ægri.

Hague, May 11, 1753.

Wm. Kersseboom.